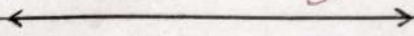
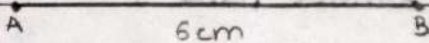


LINES - and - ANGLES

Line - A straight ~~line~~ path that extends infinitely in both directions.



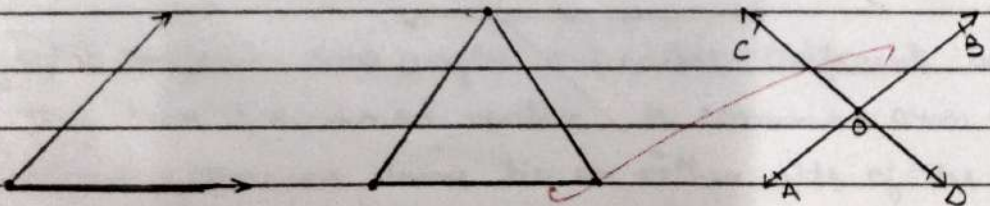
Line Segment - A line segment is a ~~fraction~~ portion of a line. Hence, it has two end points and finite length.



Ray - A ray is a part of a line that extends only in one direction. It has one end point and has no definite length.

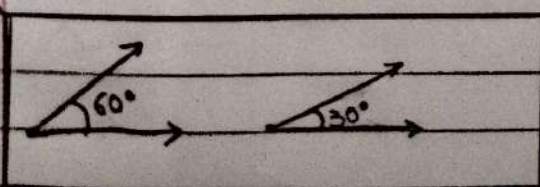


Angles - When two ~~the~~ rays, lines or line segments meet (intersect), an angle is formed. The ~~the~~ common point is called vertex.



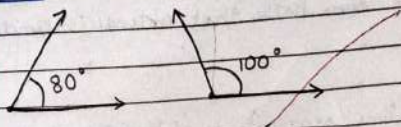
Related Angles

Complementary Angles - Two angles which add upto 90°

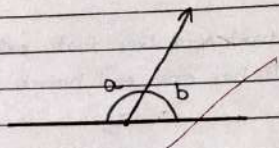


Supplementary Angles - Two angles which add upto

180°

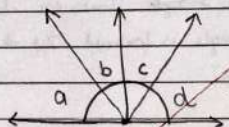


Linear Pair - Two adjacent angles which add upto 180° is called a linear pair.



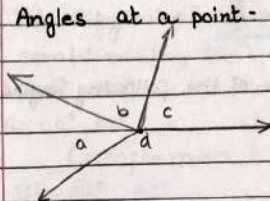
$a + b = 180^\circ$
[Linear equation]

Angle on one side of a straight line -

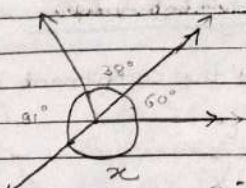


$a + b + c + d = 180^\circ$

Angles at a point -

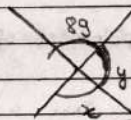
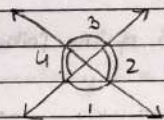


$a + b + c + d = 360^\circ$



$x = 360^\circ - (50^\circ + 30^\circ + 90^\circ)$
 $x = 171^\circ$

Vertically Opposite Angles -

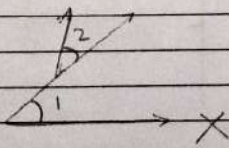
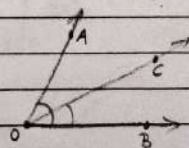
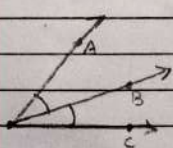


$\angle 1$ and $\angle 3$

$\angle 2$ and $\angle 4$

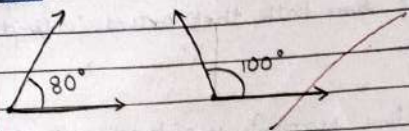
are vertically opposite

Adjacent Angles - Two angles are called adjacent angles if they have a common vertex, a common arm and their non-common arms lie on either side of the common arm.

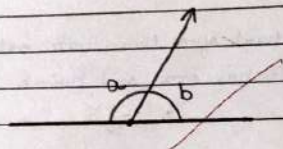


Supplementary Angles - Two angles which add upto

180°



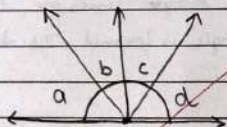
Linear Pair - Two adjacent angles which add upto 180° is called a linear pair.



$$a + b = 180^\circ$$

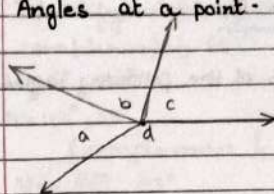
[Linear equation]

Angle on one side of a straight line -

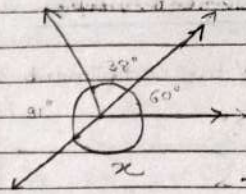


$$a + b + c + d = 180^\circ$$

Angles at a point -



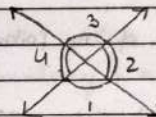
$$a + b + c + d = 360^\circ$$



$$x = 360^\circ - (50^\circ + 32^\circ + 91^\circ)$$

$$x = 171^\circ$$

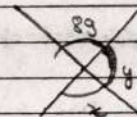
Vertically Opposite Angles -



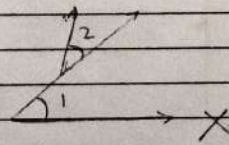
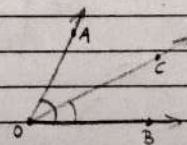
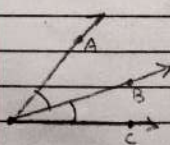
∠1 and ∠3

∠2 and ∠4

are vertically opposite

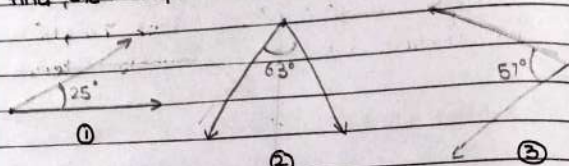


Adjacent Angles - Two angles are called adjacent angles if they have a common vertex, a common arm and their non-common arms lie on either side of the common arm.



Exercise 8.1

* Find the complement of each of the following angles:

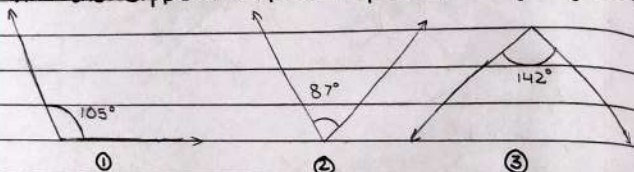


Ans-1 $\therefore 90^\circ - 25^\circ$
 $= 65^\circ$

2 $\therefore 90^\circ - 63^\circ$
 $= 27^\circ$

3 $\therefore 90^\circ - 57^\circ$
 $= 33^\circ$

* Find the supplement of each of the following angles:



Ans-1 $\therefore 180^\circ - 105^\circ$
 $= 75^\circ$

2 $\therefore 180^\circ - 87^\circ$
 $= 93^\circ$

3 $\therefore 180^\circ - 142^\circ$
 $= 38^\circ$

* Identify which of the following pairs of angles are complementary (90°) and which are supplementary (180°).

i $> 55^\circ, 125^\circ$

ii $> 34^\circ, 56^\circ$

iii $> 137^\circ, 43^\circ$

iv $> 112^\circ, 68^\circ$

v $> 45^\circ, 45^\circ$

vi $> 72^\circ, 18^\circ$

Ans $\rightarrow$ Complementary

ii $> 34^\circ, 56^\circ$

v $> 45^\circ, 45^\circ$

vi $> 72^\circ, 18^\circ$

Supplementary

i $> 55^\circ, 125^\circ$

iii $> 137^\circ, 43^\circ$

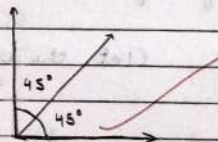
iv $> 112^\circ, 68^\circ$

* Find the x which is equal to its complement.

Ans $\rightarrow$ Complementary $x = 90^\circ$

A.T.Q

$\frac{90}{2} = 45^\circ$

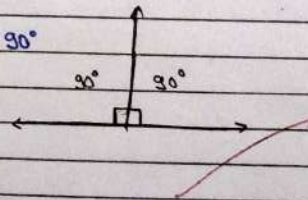


ii Find the x which is equal to its supplement.

Ans $\rightarrow$ Supplementary $x = 180^\circ$

A.T.Q

$\frac{180}{2} = 90^\circ$



* Two complementary angles are $(x+4)^\circ$ and $(2x-7)^\circ$, find the value of x .

Ans- 1st $h = (x+4)^\circ$

2nd $h = (2x-7)^\circ$

A.T.Q

$$(x+4)^\circ + (2x-7)^\circ = 90^\circ$$

$$3x - 3^\circ = 90^\circ$$

$$3x^\circ = 90^\circ + 3^\circ$$

$$x^\circ = \frac{93^\circ}{3}$$

$$x^\circ = 31^\circ$$

$$\therefore \boxed{x = 31}$$

* Two supplementary angles are in a ratio of 2:7, find the angles.

Ans- 1st $h = 2x$

(let the common ratio be x .)

2nd $h = 7x$

A.T.Q

$$2x + 7x = 180^\circ$$

$$9x = 180^\circ$$

$$x = \frac{180^\circ}{9}$$

$$\boxed{x = 20^\circ}$$

$$\therefore 1^{st} h = 2x$$

$$= 2 \times 20$$

$$= 40^\circ$$

$$2^{nd} h = 7x$$

$$= 7 \times 20$$

$$= 140^\circ$$

* Among two supplementary

* If the difference in the measures of two complementary angles is 12° , find the measure of the h .

→ Let one of the h s be x .

then the 2nd $h = (x+12)^\circ$

A.T.Q

$$x + (x+12) = 90^\circ$$

$$2x + 12^\circ = 90^\circ$$

$$2x = 90^\circ - 12^\circ$$

$$x = \frac{78^\circ}{2}$$

$$x = 39^\circ$$

$$\therefore 1^{st} h = 39^\circ$$

$$2^{nd} h = x + 12$$

$$= 39 + 12$$

$$= 51^\circ$$

* If one $\angle$ is half of its complement, find the measure of the angle.

Ans $\rightarrow$ Let the 1st $\angle$ be x .

Then the 2nd $\angle = \frac{x}{2}$

A.T.O

$$x + \frac{x}{2} = 90^\circ$$

$$\frac{3x}{2} = 90^\circ$$

$$3x = 90^\circ \times 2$$

$$x = \frac{180^\circ}{3}$$

$$x = 60^\circ$$

$$\therefore x = 60^\circ$$

$$2^{\text{nd}} \angle = \frac{x}{2} = \frac{60}{2} = 30^\circ$$

* Two adjacent angles are in a ratio of ~~5:3~~ 5:3 and they together form an angle 128° , find these $\angle$ s.

Ans $\rightarrow$ Let the common ratio be x .

$$1^{\text{st}} \angle = 5x$$

$$2^{\text{nd}} \angle = 3x$$

A.T.O

$$5x + 3x = 128^\circ$$

$$8x = 128^\circ$$

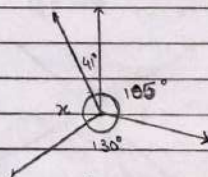
$$x = \frac{128^\circ}{8}$$

$$x = 16^\circ$$

$$\therefore 1^{\text{st}} \angle = 5x = 5 \times 16^\circ = 80^\circ$$

$$2^{\text{nd}} \angle = 3x = 3 \times 16^\circ = 48^\circ$$

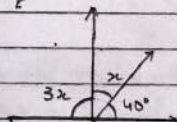
* Find the value of x in each of the following:



Ans $\rightarrow$ Total = 360°

Total of degree of $\angle$ given = 276°

Value of $x = 360^\circ - 276^\circ = 84^\circ$



Ans $\rightarrow$ A.T.O

$$3x + x + 40^\circ = 180^\circ$$

$$4x + 40^\circ = 180^\circ$$

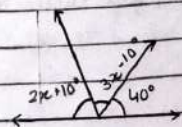
$$4x = 180^\circ - 40^\circ$$

$$x = \frac{140^\circ}{4} = 35^\circ$$

$$x = 35^\circ$$

(continued)

Ans →



= A.T.U

$$= 2x + 10^\circ + 3x - 10^\circ + 40^\circ = 180^\circ$$

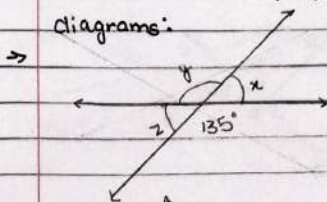
$$5x + 40^\circ = 180^\circ$$

$$5x = 180^\circ - 40^\circ$$

$$x = \frac{140^\circ}{5}$$

$$x = 28^\circ$$

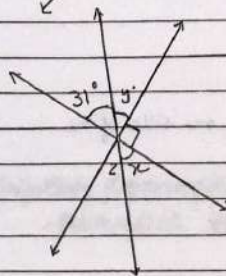
H.W

13. Find the values of x , y and z in each of the following diagrams:

$$z = 180^\circ - 135^\circ = 45^\circ \text{ (Linear pair)}$$

$$x = z = 45^\circ \text{ (vertically opposite)}$$

$$y = 135^\circ \text{ (vertically opposite)}$$

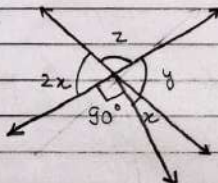


$$y = z = 59^\circ \text{ (vertically opposite)}$$

$$x = 31^\circ \text{ (vertically opposite)}$$

$$y = 180^\circ - 90^\circ - 31^\circ \text{ [Angles on the one side of a straight line]}$$

$$y = 59^\circ$$



$$2x + 90^\circ + x = 180^\circ$$

$$3x = 180^\circ - 90^\circ$$

$$x = \frac{90^\circ}{3}$$

$$x = 30^\circ$$

$$y = 2x = 2 \times 30^\circ + 60^\circ$$

$$z + y = 180^\circ$$

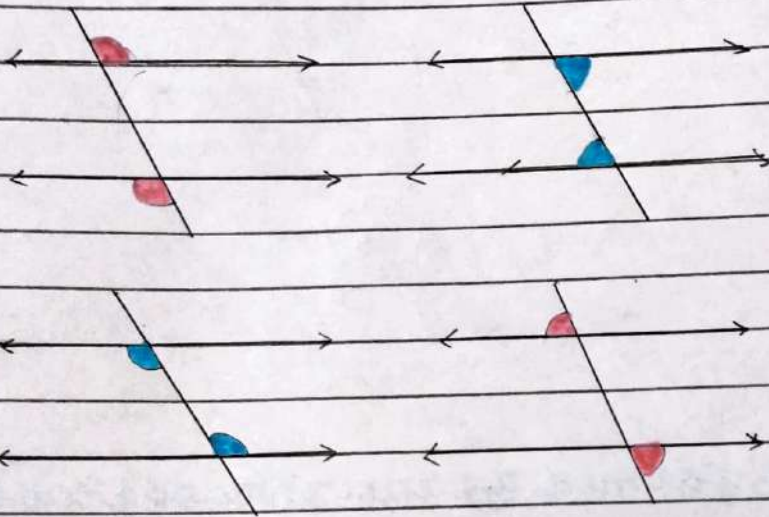
$$z + 60^\circ = 180^\circ$$

$$z = 180^\circ - 60^\circ$$

$$z = 120^\circ$$

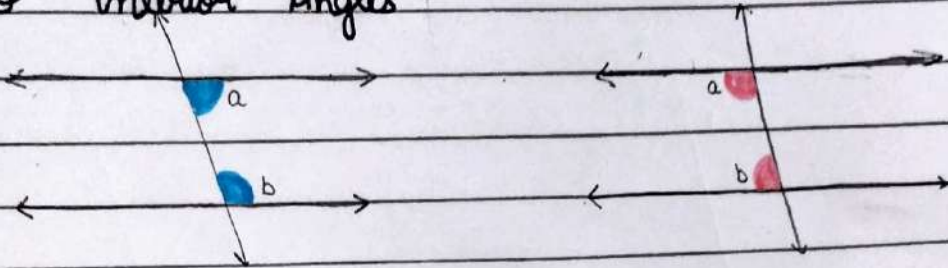
$$\therefore x = 30^\circ, y = 60^\circ \text{ and } z = 120^\circ$$

2. Alternative Angles -



NOTE - Each one of the pair of
Alternative angles are equal in
measure

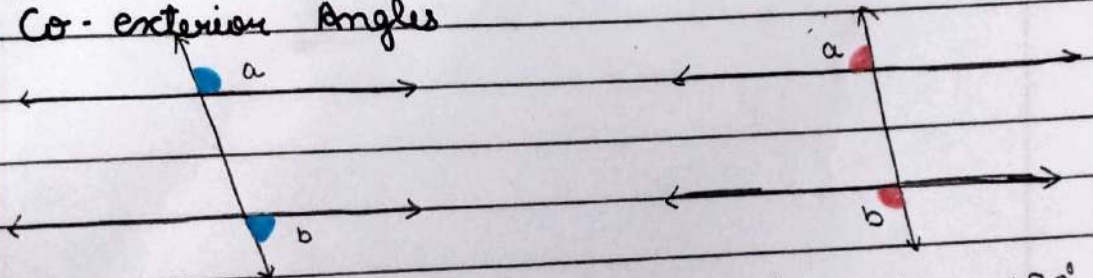
3. Co-interior Angles -



$$\therefore \angle a + \angle b = 180^\circ$$

$$\therefore \angle a + \angle b = 180^\circ$$

4. Co-exterior Angles



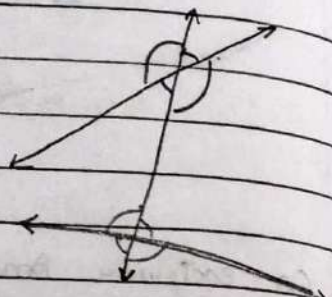
$$\therefore \angle a + \angle b = 180^\circ$$

$$\therefore \angle a + \angle b = 180^\circ$$

EXERCISE 8.2

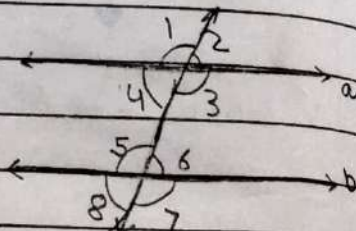
★ Identify each of the given -----
----- given figure.

- i) $\angle 2, \angle 6$ Corresponding $\angle$ s
- ii) $\angle 1, \angle 6$ none
- iii) $\angle 3, \angle 5$ Alternate interior
- iv) $\angle 2, \angle 7$ none
- v) $\angle 3, \angle 6$ Co-interior
- vi) $\angle 4, \angle 8$ corresponding



★ State ----- statements:

- i) If $a \parallel b$, then $\angle 1 = \angle 5$
→ Corresponding $\angle$ s are equal.
- ii) If $\angle 4 = \angle 6$, then $a \parallel b$.
→ Alternative ~~to~~ interior $\angle$ s are equal, so $a \parallel b$.
- iii) If $\angle 4 + \angle 5 = 180^\circ$, then $a \parallel b$.
Co-interior ~~are~~ $\angle$ s are equal, ~~so~~ then $a \parallel b$



13	14	15	16	17	18	19	20	21
M	A	M	A	M	A	M	A	M

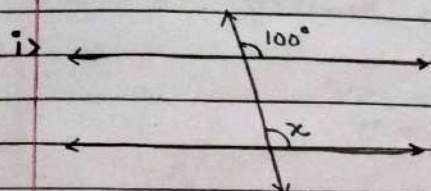
22	23	24	25	26	27	28	29	30	31
M	A	M	A	M	A	M	A	M	A

Attendance for the Months	Brought Forward
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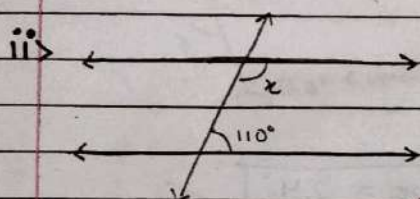
Date _____

Page _____

* In each of the following ----- value of x :

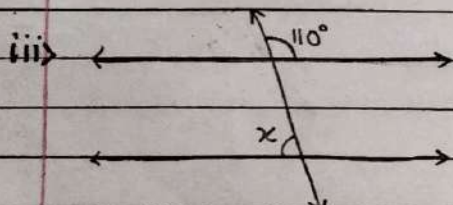


$\Rightarrow x = 100^\circ$ (Corresponding $\angle$ s are equal.)



$\Rightarrow 180^\circ - 110^\circ = 70^\circ$

$x = 70^\circ$ (Co-interior $\angle$ s add and form 180°)



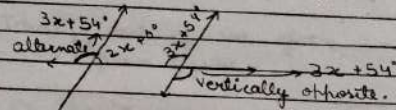
$\Rightarrow x + 110^\circ = 180^\circ$ (~~linear pair~~) (~~linear pair~~) (Supplementary)
 $\downarrow$
 (Corresponding)

$x = 180^\circ - 110$

$x = 70^\circ$

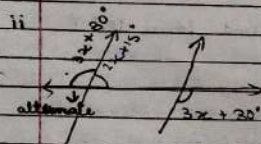
Date _____
Page _____

* In each of the following figure:



$$\begin{aligned} \Rightarrow 3x + 54^\circ + 2x + 6^\circ &= 180^\circ \\ 5x + 60^\circ &= 180^\circ \\ 5x &= 180^\circ - 60^\circ \\ x &= \frac{120}{5} \end{aligned}$$

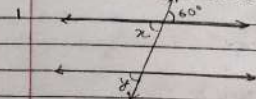
$$\boxed{x = 24^\circ}$$



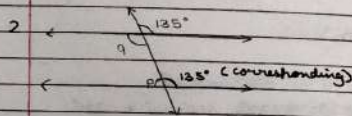
$$\begin{aligned} \Rightarrow 3x + 80^\circ + 2x + 15^\circ &= 180^\circ \\ 5x + 45^\circ &= 180^\circ \\ 5x &= 180^\circ - 45^\circ \\ x &= \frac{135}{5} \end{aligned}$$

$$\boxed{x = 27^\circ}$$

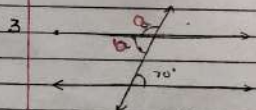
* In the following figures:



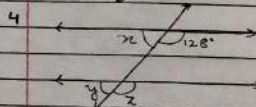
$$\begin{aligned} x &= 60^\circ \text{ (vertically opp. b.s)} \\ y &= 60^\circ \text{ (alternate exterior b.s)} \end{aligned}$$



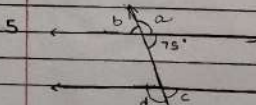
$$\begin{aligned} q &= 135^\circ \text{ (vertically opp. b.s)} \\ p &= 180^\circ - 135^\circ \text{ (supplementary)} \\ p &= 45^\circ \end{aligned}$$



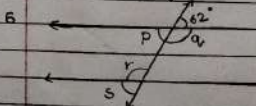
$$\begin{aligned} b &= 70^\circ \text{ (alternate)} \\ a &= 180^\circ - 70^\circ \text{ (linear pair)} \\ a &= 110^\circ \end{aligned}$$



$$\begin{aligned} x &= 128^\circ \text{ (corresponding)} \\ x &= 180^\circ - 128^\circ \text{ (linear pair)} \\ x &= 52^\circ \\ y &= 50^\circ \end{aligned}$$



$$\begin{aligned} c &= 75^\circ \text{ (corresponding)} \\ b &= 75^\circ \text{ (vertically opp. b.s)} \\ a &= 180^\circ - 75^\circ = 105^\circ \text{ (linear pair)} \\ d &= 180^\circ - 75^\circ = 105^\circ \text{ (linear pair)} \end{aligned}$$

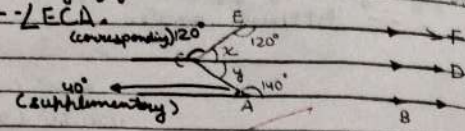


$$\begin{aligned} p &= 62^\circ \text{ (vertically opp. b.s)} \\ q &= 180^\circ - 62^\circ \text{ (linear pair)} \\ &= 118^\circ \\ r &= 118^\circ \text{ (alternate)} \\ s &= 62^\circ \text{ (corresponding)} \end{aligned}$$

Date _____
Page _____

13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	Attendance for the Months
M	A	M	A	M	A	M	A	M	A	M	A	M	A	M	A	M	A	M	A

* In the adjoining figure -----
----- $\angle ECA$.



$$x = 120^\circ - 120^\circ \text{ (supplementary)}$$

$$= 60^\circ$$

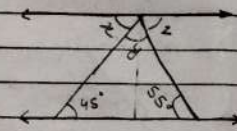
$$y = 40^\circ \text{ (alternate)}$$

$$\therefore \text{Reflex } b = 60^\circ + 40^\circ = 100^\circ$$

$$= 360^\circ - 100^\circ = 260^\circ$$

$$= 260^\circ$$

* In the adjoining figure ---
--- x, y and z.



$$x = 45^\circ \text{ (alternate)}$$

$$z = 55^\circ \text{ (alternate)}$$

$$y = \Delta \text{ sum } 180^\circ$$

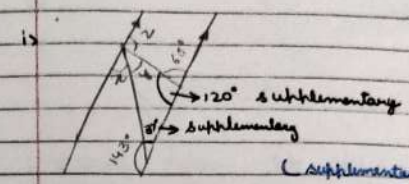
$$\rightarrow 45^\circ + 55^\circ = 100^\circ$$

$$\rightarrow 180^\circ - 100^\circ = 80^\circ$$

$$y = 80^\circ$$

Date _____
Page _____

* Calculate the measure of each lettered -----
----- arrow :



$$x = 37^\circ \text{ (alternate)}$$

$$z = 120^\circ \text{ (alternate)}$$

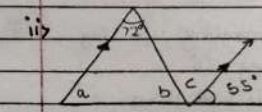
$$(Supplementary) \rightarrow y = x + z + y = 180^\circ$$

$$y = 57^\circ + 120^\circ + y = 180^\circ$$

$$y = 157^\circ + y = 180^\circ$$

$$y = 180^\circ - 157^\circ$$

$$= 23^\circ$$



$$a = 55^\circ \text{ (corresponding)}$$

$$c = 72^\circ \text{ (alternate)}$$

$$b = a + b + c = 180^\circ \text{ (supplementary)}$$

$$b = 55^\circ + b + 72^\circ = 180^\circ$$

$$b = 55^\circ + 72^\circ = 180^\circ$$

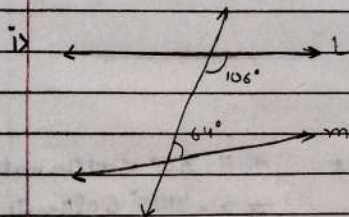
$$b = 180^\circ - 127^\circ$$

$$b = 53^\circ \text{ (supplementary)}$$

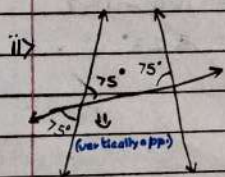
Date _____

Page _____

* In the figures given below, — or not.

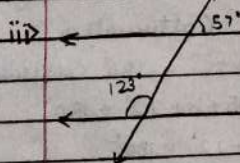


$$\begin{aligned}
 &= \angle a + \angle b = 180^\circ \\
 &= 106^\circ + 64^\circ = 170^\circ \\
 &= \text{No, hence proven } l \text{ is not } \parallel m.
 \end{aligned}$$



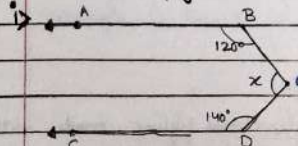
After summing up they are not forming 180° .

Hence, proven l is not $\parallel m$.

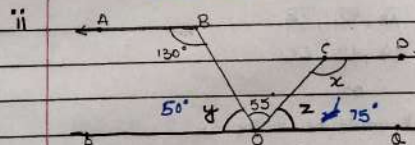


After adding they are forming 180° .
Hence, proven $l \parallel m$.

* as in the figure — — — — — x.



$$\begin{aligned}
 \angle ABO + \angle BOD + \angle ODC &= 360^\circ \\
 120^\circ + \angle BOD + 140^\circ &= 360^\circ \\
 \angle BOD + 260^\circ &= 360^\circ \\
 \angle BOD &= 360^\circ - 260^\circ \\
 \angle BOD &= 100^\circ \\
 \boxed{x = 100^\circ}
 \end{aligned}$$



$$\begin{aligned}
 \angle ABO + \angle BOP &= 180^\circ \\
 130^\circ + \angle BOP &= 180^\circ \\
 \angle BOP &= 180^\circ - 130^\circ \\
 \angle BOP &= 50^\circ \\
 y &= 50^\circ
 \end{aligned}$$

$$\begin{aligned}
 z &= 180^\circ - (y + 55^\circ) \\
 z &= 180^\circ - (50^\circ + 55^\circ) \\
 z &= 180^\circ - 105^\circ \\
 z &= 75^\circ \\
 x &= 180^\circ - 75^\circ \text{ (supplementary)} \\
 \boxed{x = 105^\circ}
 \end{aligned}$$

24/11/25